Enhancing Pre-Service Teachers’ Noticing: A Learning Environment about Fraction Concept

Pedro Ivars
Departamento de Innovación y Formación Didáctica, University of Alicante, Alicante, Spain
Pere.ivars@ua.es

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Abstract

Professional noticing allows teachers to recognise important events in a classroom and give effective responses using their knowledge. Hence developing this competence in teacher training programs is an issue in the Mathematics Education field. In this study, we present the design of a learning environment about the part-whole meaning of fraction to develop pre-service primary school teachers’ noticing of students’ mathematical thinking. The learning environment is designed around three tasks (vignettes) that pre-service teachers have to analyse using knowledge from research on mathematics education provided as a students’ hypothetical learning trajectory. Eighty-five pre-service primary school teachers participated in this learning environment. Pre-service teachers’ written answers to the three tasks are the data of this study. Results allow us to characterise the enhancement of pre-service teacher noticing through looking at the changes in the discourse generated in the three tasks.

Keywords: fraction; hypothetical learning trajectory; pre-service teacher; representations of practice; teacher noticing.

1. INTRODUCTION

During a mathematics lesson, a teacher faces overlapping situations and interactions simultaneously, hindering their attention to all of them. In this context, teachers should focus their attention on those classroom situations or interactions that could potentially enrich students’ mathematical learning (Mason, 2002; van Es, & Sherin, 2002). In fact, NCTM (2014) points out that teaching effectively implies that teachers “elicit evidence of students’ current mathematical understanding and use it as the basis for making instructional decisions” (p. 53). From this perspective, effective teaching implies observing students, listening attentively to their ideas and explanations, planning objectives and using the information to make instructional decisions.

Therefore, teachers must develop greater flexibility in recognising students’ mathematical thinking while teaching (van Es, & Sherin, 2002) and must be
aware of what happens in their classrooms and how to manage it (Mason, 2002; 2020). In this context, teacher noticing has been conceptualised as a competence that allows teachers to recognise important events in a classroom and give effective responses (Mason, 2002). Hence, a line of research has emerged trying to identify tools and contexts to develop teacher noticing (Fernández & Choy, 2020).

### a. Professional noticing

A professional vision is the ability to see certain phenomena in a particular way which distinguishes a professional or expert in a certain area from someone who is not (Goodwin, 1994). In the case of mathematics teaching, a professional vision (or professional noticing) allows teachers to identify relevant aspects in a teaching-learning situation that non-professional people would not be able to identify (Roller, 2016) and reason about the situation using mathematical knowledge and knowledge of the teaching and learning of mathematics. Sherin (2007) characterised this competence as two sub-processes: selective attention (noticing) and knowledge-based reasoning. Selective attention is linked to the teachers’ ability to focus their attention on a particular classroom situation relevant to students’ learning. Knowledge-based reasoning is linked to the teachers’ ability to use their available knowledge to make sense of this classroom situation. Therefore, this competence helps teachers connect theoretical knowledge with practice (Brown, Fernández, Helliwell, & Llinares 2020; Seidel, Stürmer, Prenzel, Jahn, & Schäfer, 2017).

Jacobs, Lamb, and Philipp (2010) particularised professional noticing of children’s mathematical thinking as a set of three interrelated skills: attending to children’s strategies, interpreting children’s understanding, and deciding how to respond on the basis of children’s understanding. This competence is understood as a knowledge-based reasoning since teachers must attend to a classroom situation and then interpret the situation, considering their available knowledge (Sherin, 2007) to decide what to do next. Therefore, this competence highlights the need of specialised knowledge (Thomas, Jong, Fisher, & Schack, 2017).

Professional noticing of children’s mathematical thinking implies the teachers’ ability to use their knowledge (mathematical content knowledge and pedagogical content knowledge) to attend to, interpret and decide what to do next (Fernández & Choy, 2020; Thomas et al., 2017). When pre-service teachers notice children’s mathematical thinking (attending to, interpreting and deciding), they have to use their knowledge (subject matter knowledge and pedagogical content knowledge).

### b. Professional noticing as a knowledge-based reasoning competence

Brown et al., (2020) linked the different domains of the Mathematical Knowledge for Teaching framework
c. Developing teacher noticing

In recent years, an important line of research has emerged examining contexts and tools for pre-service teachers noticing development in teacher training programs (Fernández & Choy, 2020; Shack et al., 2017). These studies have shown that using representations of practice, such as videos of classroom interactions or transcriptions of students' written responses, is a favourable context for its development (Ivars, Fernández, & Llinares, 2020; Ivars, Fernández, Llinares, & Choy, 2018; Sánchez-Matamoros, Fernández & Llinares, 2015; 2019; Schack et al., 2013; van Es & Sherin, 2008). Other contexts that can also support its development are writing narratives during their period of practice at schools (Fernández, Llinares, & Rojas, 2020; Ivars & Fernández, 2018), online discussions and tutor feedback (Fernández, Llinares, & Valls 2012; Ivars & Fernández, 2018; Llinares & Valls, 2010). Results from these studies have shown that this competence can be developed in teacher training programmes although its development is not an easy task without a frame that guides pre-service teachers noticing (Fernández & Choy, 2020), such as the students' learning trajectories (Sztajn & Wilson, 2019).
d. Hypothetical Learning Trajectories

Learning trajectories have been conceptualised from different perspectives (Lobato & Walters, 2017). Nevertheless, a shared assumption is that a learning trajectory articulates the students’ conceptual progress from informal thinking to a more sophisticated mathematical reasoning. Following Simon (1995), a Hypothetical learning trajectory (HLT) is made up of three components: a learning goal, learning activities, and a hypothetical learning process (levels of understanding).

Previous research has shown that students learning trajectories could provide pre-service teachers with a structured framework to focus their attention on students’ thinking (Edgington, 2014; Edgington, Wilson, Sztajn, & Webb, 2016), since they can support pre-service teachers in identifying learning goals in the instructional activities, in interpreting students’ mathematical thinking and in responding with appropriate instruction (Ivars et al., 2018; Sztajn, Confrey, Wilson, & Edgington, 2012). Furthermore, learning trajectories can provide pre-service teachers with a mathematical language to describe students’ thinking (Edgington et al., 2016).

e. Using vignettes in teacher training programs

To connect theoretical knowledge with mathematics teaching practice in teacher training programs, researchers design learning environments to provide pre-service teachers with opportunities to learn about and for practice. (Fernández Sánchez-Matamoros, Valls, & Callejo, 2018). In our research group (GIDIMAT-UA), these learning environments are designed using vignettes. A vignette includes a representation of practice, some questions to guide its analysis and information from previous research on students’ mathematical understanding of the mathematics concept. This information can be provided as a student’s hypothetical learning trajectory. This information provides pre-service teachers with the theoretical knowledge required to analyse the representation of practice.

Representations of practice are understood as depicting a classroom situation (e.g. a transcription of students’ answers to an activity, or a cartoon showing an interaction teacher-student) to promote pre-service teachers’ reflection and discussion of real-life contexts. A representation of practice can represent one aspect or several aspects of a class situation, but not all the characteristics of a class (Buchbinder & Kuntze, 2018). This reduction of information makes the vignettes useful instruments in the professional development of teachers in multiple ways (Skilling & Stylianides, 2019) since they allow teachers to focus the attention on those aspects of the practice object of learning. Furthermore, they can be designed in different formats (Friesen & Kuntze, 2018): video recordings of real classroom situations (van Es & Sherin,
2008), student responses to different problems or dialogues between the teacher and the students solving various problems (Fernández et al., 2018; Ivars et al., 2020) or animations or cartoons (Herbst & Kosko, 2014).

Research has shown that vignettes provide teachers with real contexts to analyse and interpret aspects of the teaching and learning of mathematics and provide them with opportunities to relate theoretical ideas about the teaching and learning of mathematics with examples from practice (Buchbinder & Kuntze, 2018; Fernández et al., 2018).

Results from our research group have shown that these learning environments using vignettes support pre-service teachers’ attention on important aspects of students’ understanding, and therefore help them develop the competence of noticing (Buforn, Llinares, Fernández, Coles & Brown, 2020; Fernández et al., 2012; Fernández, Sánchez-Matamoros, Moreno, & Callejo, 2018; Ivars et al., 2018; Ivars et al. 2020; Sánchez-Matamoros et al., 2019). Following, we will present an example of a learning environment related to the part-whole meaning of fraction, which is part of a pre-service primary school teachers’ training programme.

f. A part-whole meaning of fraction learning environment

This learning environment is organised around six sessions lasting two hours each (Figure 1, Ivars, 2018). In the first two sessions, we introduced the mathematical elements related to the part-whole meaning of fraction to pre-service teachers. They had to solve some fraction activities and analysed video-clips of students solving fraction activities. In the last four sessions, we introduced the learning trajectory of the part-whole meaning of the fraction concept. Pre-service teachers had to analyse three vignettes, using the theoretical information provided in a HLT.

Figure 1. Learning environment of the part-whole meaning of fraction
The HLT is provided as a theoretical document and includes: a primary school students’ hypothetical learning process (levels of understanding, Figure 2), examples of primary school students’ answers reflecting characteristics of each of the levels of understanding (Figure 3) and examples of activities that could help students progress in their understanding of the concept of fraction as a part-whole (Figure 4). The HLT is designed by considering the previous research on how students’ reasoning about fractions develops over time (Battista, 2012; Steffe & Olive, 2010). This theoretical document provides pre-service teachers with the theoretical knowledge (about fractions and the teaching and learning of fractions) they need to identify noteworthy mathematical aspects of the representation of practice, interpret them and support their teaching decisions.

**Level 1. Students cannot identify and represent fractions**
- Not recognising that the parts into which the whole is partitioned must be of equal size
- Not keeping the same whole when comparing fractions

**Level 2. Students can identify and represent proper fractions**
- Recognising that the parts into which the whole is partitioned must be of equal size (but not necessarily of the same shape)
- Using unit fractions as iterative units to construct proper fractions
- Keeping the same whole to compare fractions
- Not recognising that a part can be divided into other parts

**Level 3. Students can identify and represent fractions**
- Recognising that a part can be divided into other parts
- Using fractions as iterative units to construct fractions
- Recognising that the size of a part decreases when the number of parts increases

Figure 2. Students’ hypothetical learning process

Figure 3 shows some examples of primary school students' answers included in the HLT reflecting characteristics of level 2. Student 1’s answer shows difficulties in comparing fractions since he/she does not keep the same whole when comparing. Student 2’s answer reflects difficulties in representing the improper fraction by not identifying the unit fraction 1/4 as an iterative unit. These are characteristics of level 3.
The HLT also includes examples of activities that could help primary school students progress in their understanding of the part-whole meaning of fraction. Figure 4 shows an activity that can help students progress from level 2 to level 3 of understanding according to the HLT). The activity aims at using the unit fraction as an iterative unit to construct fractions.

The following section details the characteristics of the vignettes used in this learning environment and shows vignette 2 as an example.

g. A vignette of comparing fractions

The vignettes of the learning environment include three elements: i) transcriptions of primary school students' answers to a fraction activity showing different levels of understanding (students' names are pseudonyms), ii) guiding questions related to the three skills that articulate the competence of noticing: identifying mathematical elements, interpreting students' understanding and making teaching decisions to support students' progress in their understanding, and iii) the theoretical documents with the HTL explained before.

Vignette 2 consists of an activity of comparing fractions, the answer of three primary school students (showing different characteristics of the levels of understanding shown in the HLT), the
HLT as a theoretical document and four guiding questions:

1. Which is greater 4/5 or 3/4? Explain it with a picture or your words

(Answer of Ana and Iván)
Iván: Well we think 4/5 is greater than 3/4
Teacher: And how do you know?
Ana: Because we have drawn four fifths, which is... and three quarters that is... (while she was drawing on the blackboard the following images):

Teacher: And?
Iván: Well, so you can see that 4/5 is greater than ¾
Teacher: Do you all agree? ... Vicent? What do you think?

(Answer of Marta and Vicent)
Vicent: Well, we agree, but we've done it differently.
Teacher: Could you show us how have you done it?
Marta: Yes, look, here we have 4/5 that represents four out of five (while she was drawing the following figure):

And, then we have ¾ which also represents three out of four that is...
(She draws the following figure):

Teacher: What do you think? Has anyone done it in another way? No one? Can someone else explain, differently, that 4/5 is greater than ¾?

(Answer of Núria and Louis)
Louis: Yes, of course ... we can but... we have not drawn it
Teacher: What have you done?
Núria: Well we thought that 4/5 needs 1/5 to complete the whole and ¾ needs ¼ to complete it. Therefore... as 1/5 is smaller than ¼, then 4/5 is greater than ¾ because it needs less to complete the whole than ¾.
Louis: That's it!

h. Guiding questions
- **Q1-** Describe the activity considering the learning objective: what are the mathematical elements that the student needs to solve it?
- **Q2-** Describe how each pair of students has solved the activity identifying how they have used the mathematical elements involved and the difficulties they have had with them.
• **Q3-** What are the characteristics of students’ understanding (levels of understanding of the Hypothetical Learning Trajectory) that can be inferred from their responses? Justify your answer.

• **Q4-** How could you respond to these students? Propose a learning objective and a new activity to help students progress in their understanding of fractions.

The mathematical elements that should be considered to solve this activity of comparing proper fraction are the wholes must be the same to compare and the inverse relationship between the number of the parts and the size of each part (a bigger number of parts makes smaller parts). The answer of Ana and Iván show characteristics of level 2 since they identify that the wholes must be the same to compare fractions (they represent both fractions using the same whole). Nevertheless, their answer does not show characteristics of understanding the inverse relationship between the number of the parts and the size of each part (since their answer relies on the graphical representation). The second couple, Marta and Vicent, shows characteristics of the level 1 since they do not keep the same whole to compare both fractions nor show understanding of the inverse relationship. This couple provides a correct answer but using an incorrect reasoning. Finally, Núria and Louis answer focuses on the inverse relationship between the number of the parts and the size of each part as they stated that “[…] 4/5 needs 1/5 to complete the whole and ¾ needs ¼ to complete it”. Therefore they show characteristics of level 3.

2. **METHODOLOGY**

a. **Participants**

In this learning environment participated 85 pre-service primary school teachers (PTs) enrolled in a university course related to the teaching and learning of mathematics during their third out of the four years of the degree to become a primary school teacher.

b. **Instrument and data collection**

During the learning environment PTs solved the three vignettes individually. Data of this research were PTs’ written answers to questions Q2, Q3 and, Q4 to the three vignettes. To maintain participants’ anonymity we named PTs as: PT1, PT2.... PT85.

c. **Analysis**

We made a qualitative analysis of PTs’ answers to the three vignettes in two phases. In the first phase, three researchers analysed PTs’ answers, individually, according to whether they (i) identified the mathematical elements in the student’s answers; (ii) interpreted the student’s understanding considering the HLT and the mathematical elements...
identified; and (iii) provided activities that helped students progress in their understanding. We then compared our results and discussed our discrepancies (triangulation process) until we reached an agreement. From the analysis of (i) and (ii), we identified three categories (groups of PTs) regarding the details identified and how they interpreted students' understanding:

- **Non-evidencers**: PTs who interpreted students' understanding but did not provide details from students' answers to support their interpretations.
- **Adders**: PTs who interpreted students' understanding providing details from students' answers, but they added information that cannot be inferred from students' answers.
- **Evidencers**: PTs who interpreted students' understanding providing details from students' answers to support their interpretations.

Then, we analysed whether each group of PTs provided activities focused on students' conceptual progression. In the second phase, we analysed changes in PTs' answers along the three vignettes. These changes provided us with information to characterise PTs noticing enhancement.

3. RESULTS

a. Interpreting and deciding relationship

Our results highlight that those PTs who provided a more detailed discourse to support their interpretations (Evidencers) were more able to provide activities to support students' conceptual progression in the three vignettes. We are going to show this relationship in the vignette of comparing fractions as an instance of this result.

In the task of comparing fractions, 71 out of the 85 PTs interpreted students' understanding, while 14 did not interpret it since they only provided descriptive answers. Fifty-four out of the 71 PTs who interpreted students' understanding provided details from students' answers to support their interpretations (Evidencers) and 17 out of the 71 PTs did not provide details to support their interpretations (Non-evidencers).

For instance, PT23 interpreted students' understanding as follows (emphasis added to the mathematical elements identified):

**Ana and Ivan** \(\rightarrow\) They are at level 2 since when they compare fractions, they recognise that the wholes must be the same.

**Marta and Vicent** \(\rightarrow\) They are at level 1 since they do not keep the same whole when they compare fractions.

**Louis and Núria** \(\rightarrow\) They are at level 3 since when comparing fractions they recognise that the wholes must be the same and establish the inverse relationship between the number of the parts and the size of each part.

This PT identified the mathematical elements in students' answers, (e.g. "when they compare fractions recognise that the wholes must be the same" or "They establish the inverse relationship between the number of the parts and...".)
the size of each part”) and interpreted students’ mathematical thinking recognising the relationship between those mathematical elements and the different levels of the HLT. Nevertheless, he did not provide details from students’ answers to support their interpretations (Non-evidencer).

On the other hand, PT73 interpreted students’ understanding as follows (emphasis added to the mathematical elements identified):

**Ana and Ivan** → They are at level 2 since they keep the same whole when they represent both fractions. Then they compare both areas to provide the answer.

**Marta and Vicent** → They are at level 1. When they represent both fractions, they only notice four shaded parts in 4/5 and three shaded parts in ¾. Therefore, although they provide a correct answer the reasoning is not correct because they do not keep the same whole when comparing fractions.

**Louis and Núria** → Level 3

These students use the mathematical element inverse relationship between the number of the parts and the size of each part, to justify their answer since they stated “…4/5 is greater than 3/4 because it needs less to complete the whole than ¾ needs”.

PT73 identified the mathematical elements in students’ answers and interpreted students’ mathematical thinking recognising the relationship between those mathematical elements and the different levels of HLT. Moreover, she provided details from students’ answers to support her interpretations. For instance when she wrote that Marta and Vicent do not keep the same whole when comparing fractions and they “[...] only notice four shaded parts in 4/5 and three shaded parts in ¾. Therefore, although they provide a correct answer the reasoning is not correct [...]”. She also interpreted students’ understanding of the inverse relationship providing details from students’ answer when she stated that Louis and Núria use this mathematical element to “justify their answer since they stated “…4/5 is greater than 3/4 because it needs less to complete the whole than ¾ needs”.

Excerpts from the answers, such as the ones from PT73 (Evidencer) and PT23 (Non-evidencer) show the different ways in which PTs interpreted students understanding in this task.

Regarding the activities provided, 26 out of the 54 PTs, who interpreted students thinking providing details (Evidencers), proposed at least one activity to help students progress in their understanding of fractions (48%). On the other hand, five of the 17 PTs who did not provide details in their interpretations (Non-evidencers), proposed at least one activity (29%).

In this context, the Non-evidencer PTs provided activities that were not related to the objective proposed or without sense. For instance, with the objective of understanding that the wholes must be the same to compare fractions, PT23 provided an activity of representing fractions and partitioning the whole that was not related with the objective proposed:
**Objective:** Recognise that the whole must be the same when comparing fractions.

**Activity:** We have two equal paper sheets and we want to divide one of them in $\frac{1}{4}$ and the other in $\frac{1}{2}$.

On the other hand, PTs in the Evidencer group provided activities connected with the learning objective that could help students progress in their understanding. For instance, PT73 provided the following activity, focused on comparing unitary fractions, to help Ana and Iván understand the inverse relationship between the number of parts and its size. This activity provides students various unitary fractions of the same whole. Hence, it requires PTs comparing the number of the parts of the denominator and realising that a bigger number of parts in the denominator makes each part smaller:

**Objective:** To understand the inverse relationship between the number of the parts and the size of each parts; a bigger number of parts makes smaller parts.

**Activity:** Jose, Rosa and Carlos buy the same cake. Jose eats $\frac{1}{3}$ of his cake, Rosa eats $\frac{1}{4}$ of her cake and Carlos eats $\frac{1}{5}$ of his cake. Who do eat more cake? Explain it.

In the next section, we present how these different ways of interpreting changed through the learning environment.

### b. Noticing enhancement

Through the three vignettes (Table 1), 42 PTs consistently provided a detailed discourse (Evidencers), and 10 PTs provided a non-detailed discourse (Non-evidencers). Twenty-eight PTs improved their discourse since they shifted from Non-evidencers or Adders to Evidencers. This discourse' improvement was followed by an improvement of PTs' ability to provide activities according to students' understanding (from 34% in the first vignette to 63% in the last, see Table 2). However, five PTs, showed a regression since they changed from Evidencers or Adders to Non-evidencers.

<table>
<thead>
<tr>
<th>Ways of interpreting students' mathematical thinking</th>
<th>Discourse progress</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>From Non-evidencer or Adder to Evidencer</td>
</tr>
<tr>
<td>Interpreting through the three tasks</td>
<td>12</td>
</tr>
<tr>
<td>Difficulties in at least one task</td>
<td>16</td>
</tr>
<tr>
<td>Total</td>
<td>28</td>
</tr>
</tbody>
</table>

Table 1. Pre-service teachers discourse progress in the learning environment

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Table 2. Number of activities provided in each task considering the discourse provided

<table>
<thead>
<tr>
<th>PTs</th>
<th>Number of activities in Task 1</th>
<th>Number of activities in Task 2</th>
<th>Number of activities in Task 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>From Nonevidencer/Adder to Evidencer</td>
<td>(28) 19 (34%)</td>
<td>14 (25%)</td>
<td>35 (63%)</td>
</tr>
<tr>
<td>Always Non-evidencer</td>
<td>(10) 4 (20%)</td>
<td>2 (10%)</td>
<td>9 (45%)</td>
</tr>
<tr>
<td>From Evidencer/Adder to Nonevidencer</td>
<td>(5) 4 (40%)</td>
<td>2 (20%)</td>
<td>2 (20%)</td>
</tr>
<tr>
<td>Always Evidencer</td>
<td>(42) 45 (54%)</td>
<td>21 (25%)</td>
<td>49 (58%)</td>
</tr>
</tbody>
</table>

4. DISCUSSION AND CONCLUSION

Our results allowed us to characterise the enhancement of teacher noticing through PTs changes in the discourse generated, since the progress in the discourse, considering the details used to support their interpretations, influenced PTs ability to propose activities.

These results suggest a relationship between the discourse provided by PTs interpretations of students’ mathematical understanding and the activities provided; PTs who produced a more mathematical detailed discourse to interpret students’ understanding proposed more activities according to students’ understanding. Therefore, the value of a detailed mathematical discourse can be seen “as a major learning outcome in its own right” (Clarke, 2013, p. 22). In this sense, “the more sensitive you are to noticing details, the more tempted you are likely to be to act responsively” (Mason, 2002, p. 248). Consequently, it seems that producing a detailed discourse may be distinctive in enhancing noticing. Our results seem to suggest that a detailed-sensitive discourse leads PTs to a more attentive focus on students’ understanding and prepares them to make instructional decisions based on students’ mathematical understanding.

The regression of some PTs can be explained by the difficulties interpreting some of the mathematical elements of the fraction concept in the vignettes. This highlights the critical role played by mathematical content knowledge in the enhancement of teacher noticing.

Furthermore, our results show that the characteristics of the vignettes used and the HLT supported PTs to link theoretical knowledge and practice, and helped them improve their professional discourse. This improvement can be seen as evidence of PTs noticing enhancement since PTs who generated a more detailed discourse to interpret students' understanding, were more able to provide an activity to support students' conceptual progression. Nevertheless, the enhancement of noticing is challenging and remains dependent on PTs' mathematical content knowledge, since the mathematical elements linked to each vignette generated different difficulties in PTs.
We are aware that we cannot generalise our results, and more research is necessary to analyse how PTs’ noticing develops during teacher training programs. In future projects, it will be interesting to analyse how PTs use the knowledge learned during the university courses in their internship period at the schools to notice children’s mathematical thinking.

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